## Overview

- What is absolute risk?
- Counseling
- Cancer prevention in the population
- Do SNPs add much in these applications?

| Absolute Risk for Breast Cancer |  |
| :--- | :--- |
| Computed from Gail et al., JNCI, 1989 |  |
| age $\mathbf{4 0}$ |  |
| Menarche age 14 | baseline risk |
| Nulliparous | increased risk |
| No biopsies | baseline risk |
| Mother had breast cancer | increased risk |
| What is the chance that this woman will |  |
| be diagnosed with breast cancer by age |  |
| $70 ? ~ 0.116(11.6 \%)$ |  |



## Using Risk Models to Counsel Women for Early Detection or Prevention

- General perspective on risk
- Formal weighing of risks and benefits

Should a Woman in her Forties Have Screening Mammography?

- US Prev. Services Task Force (AIM, 2009)
- "recommends against routine screening mammography in women aged 40 to 49 years."
- No factors except age and deleterious mutations "conveys a clinically important absolute increased risk for cancer."
- Decision based instead on "patient context, including the patient's values regarding specific benefits and harms."


## Counter-example

A 40-year old woman is uncertain whether to have screening mammograms. Her mother and sister had breast cancer. Her 5 -year absolute risk (1.8\%) exceeds that of a 50 -year old woman without risk factors (0.6\%).

## Women in Their Forties with the Breast Cancer Risk of a 50-Year Old Woman with No Risk Factors

- Non-Hispanic White Women 11.6 million (74\%)
- Non-Hispanic Black Women 0.85 million (31\%)

Wu, Graubard, Gail AIM 2012

Weighing the Risks and Benefits of Tamoxifen

Gail, Costantino, Bryant, Croyle, Freedman, HelzIsouer, Vogel, JNCI 1999; 91:1829-46

| TAMOXIFEN EFFECTS ON LIFE-THREATENING EVENTS |  |
| :---: | :---: |
|  | RR (95\% CI) |
| INVASIVE BREAST CANCER | 0.51 (0.39-.66) |
| HIP FRACTURE | 0.55 (0.25-1.1) |
| ENDOMETRIAL CANCER |  |
| <50 | 2.5 (1.4-5.0) |
| 50+ | 4.0 (1.7-11) |
| STROKE | 1.6 (0.9-2.8) |
| PULMONARY EMBOLUS | 3.0 (1.2-9.3) |
| Fisher et al, JNCI, 1998 |  |




| NET BENEFIT INDEX* FOR 10,000 WOMEN WITH UTERI OVER 5 YEARS |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| INVASIVE | WHITE |  | BLACK |  |
| BREAST CA | 40-49 | 50-59 | 40-49 | 50-59 |
| RISK (5 YEARS) |  |  |  |  |
| 2\% | 73 | -75 | 14 | -187 |
| 4\% | 196 | 38 | 137 | -74 |
| 6\% | 318 | 149 | 259 | 37 |
| *Net number of life the net number of | hreaten evere e | events $p$ spreven | ented plus | s half |


| Benefit/risk indices for tamoxifen and raloxifene for white non-Hispanic women with a uterus |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 5.year risk | Tamoxifen |  |  | Raloxifene |  |  | Strong evidence ofbenefits outweighingrisksModerate evidence ofbenefits outweighingrisksBenefits do notoutweigh risks |
|  | 50.59 | 60.69 | 70.79 | 50.59 | 60.69 | 70.79 |  |
| 1.5 | -133 | . 310 | ${ }^{325}$ | ${ }^{21}$ | 11 | 15 |  |
| 20 | - 105 | ${ }^{233}$ | ${ }^{28}$ | ${ }^{43}$ | 1 | 7 |  |
| 2.5 | 78 | ${ }^{255}$ | ${ }^{271}$ | ${ }^{\text {a }}$ | ${ }^{33}$ | ${ }^{29}$ |  |
| ${ }^{3} 0$ | 5 | ${ }^{228}$ | ${ }^{24}$ | ${ }_{86}$ | ${ }_{55}$ | 51 |  |
| ${ }^{3.5}$ | ${ }^{25}$ | ${ }^{202}$ | ${ }^{217}$ | 108 | ${ }^{76}$ | 7 |  |
| 4.0 | 3 | .175 | . 190 | ${ }^{128}$ | ${ }_{9}$ | ${ }^{9}$ |  |
| 4.5 | ${ }^{29}$ | ${ }^{148}$ | 1184 | 150 | ${ }^{19}$ | ${ }^{115}$ |  |
| 5.0 | ${ }_{56}$ | -121 | 137 | 172 | ${ }_{1} 40$ | ${ }^{136}$ |  |
| 5.5 | ${ }^{83}$ | 5 | 111 | 193 | 161 | ${ }^{157}$ |  |
| 6.0 | ${ }^{109}$ | 60 | 8 | 214 | 183 | 179 |  |
| ${ }_{6} .5$ | ${ }^{135}$ | 4 | . 58 | ${ }^{238}$ | 204 | ${ }^{198}$ |  |
| 7.0 | 182 | 15 | ${ }_{3}$ | 256 | 225 | ${ }^{22}$ |  |
| $\underset{\substack{\text { 5.veaf proieade } \\ \text { risk of ficis }}}{ }$ | Cuidian | crid dase | $\overline{w+1}$ | Combining using WHI | tiom |  |  |
| Freedman | Netal | 2011: | 9:2327-2 |  |  |  | mansorancalococor |

## Risk Models in Population Cancer

## Prevention

- Designing prevention trials
- Assessing population absolute risk reduction from prevention strategies
- "High risk" strategy for interventions with adverse side-effects
- Allocation of preventive resources under cost constraints



## Some SNPs Associated with Breast Cancer

| Location | Disease Allele <br> Frequency | Odds Ratio per <br> Allele | Reference |
| :--- | :---: | :---: | :---: |
| FGFR2 | 0.38 | 1.26 | 1 |
| TNRC9 (or TOX3) | 0.25 | 1.20 | 1 |
| MAP3K1 | 0.28 | 1.13 | 1 |
| LSP1 | 0.30 | 1.07 | 1 |
| CASP8 | 0.87 | 1.136 | 2 |
| 8q | 0.40 | 1.08 | 1 |
| 2q35 | 0.497 | 1.20 | 3 |
|  |  | Geometric mean |  |
|  |  | 1.15 |  |

1. Easton et al., Nature 2007;447:1087-1095
2. Cox et al., Nature Genetics 2007;39:352-358
3. Stacey et al., Nature Genetics 2007;39:865-869

Comparisons of Discriminatory Accuracy

| Model | Age-specific AUC |
| :--- | :---: |
| 7-SNPs | 0.574 |
| 11-SNPs | 0.585 |
| 18-SNPs | 0.587 |
| "Foreseeable SNPs" (70) | 0.635 |
| BCRAT | 0.607 |
| BCRAT+ 7-SNPs | 0.632 |
| BCRAT+11-SNPs | 0.637 |
| BCRAT+ "Foreseeable SNPs" | 0.670 |
| BCRAT + Mam. Density | 0.654 |

## Risk Models in Population Cancer

## Prevention

- Designing prevention trials
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Decision to Take Tamoxifen in 100,000 Women with Uteri, Aged 50-59

| Health <br> Outcome | Relative Risk | \# Cases If <br> No Tamoxifen | \# Cases If All <br> Tamoxifen |
| :--- | :---: | :---: | :---: |
| Invasive Br. <br> Ca. | 0.51 | 246.6 | 125.8 |
| Hip Fracture | 0.55 | 101.6 | 55.9 |
| Endometrial <br> Ca. | 4.01 | 81.4 | 326.4 |
| Stroke | 1.59 | 110 | 174.9 |
| Pulmonary <br> Emb. | 3.01 | 50 | 150.5 |
| Total |  | 589.6 | 833.5 |

## Threshold Risk r* for Optimal Decision

- Only women with risk $r^{*}>774.3 / 10^{5}$ have a positive net expected benefit from tamoxifen
- Only about $1 \%$ of this population has a risk this high
- Very small "high risk group" means limited potential for prevention, unless practically all the cancers arise from this small group


## Life-Threatening Events per Year in $10^{5}$ 50-59 Year Old Women with Uteri with Various Prevention Strategies

| Strategy | Expected Life- <br> Threatening Events <br> (Improvement) |
| :--- | :---: |
| None get tamoxifen | 589.6 |
| BCRAT $>$ r $^{\star}=744 / 10^{5}$ | $588.2(-1.4)$ |
| BCRAT+7 SNPs $>$ r $^{*}$ | $587.8(-1.8)$ |
| Perfect Breast Cancer Model | $469.7(-119.9)$ |

## Approaches to Improve the High-Risk Strategy

- Improve the interventions
- Less toxic
- More effective in preventing breast cancer
- Improve discriminatory accuracy of the breast cancer risk model
- Model the risks of the other health outcomes affected by the intervention, such as stroke (Gail, SIM 2012)


## Risk Models in Population Cancer Prevention

- Designing prevention trials
- Assessing population absolute risk reduction from prevention strategies
- "High risk" strategy for interventions with adverse side-effects
- Allocation of preventive resources under cost constraints


| Mammography strategies based on risk if only enough <br> money to give mammograms to half the population |  |
| :--- | :--- |
| mammograms | Mammograms <br> at random |
| Allocation by |  |
| BCRAT rank |  | | Allocation by |
| :--- |
| BCRAT +7 SNPs rank |

## Absolute Risk Models in Prevention - Summary

- Counseling patients
- General perspective
- Weighing favorable and unfavorable effects of preventive interventions
- Public health applications
- Designing prevention trials
- Assessing potential absolute risk reduction from preventive interventions
- Implementing "high risk" prevention strategy
- Allocating scarce resources
- Need stronger risk factors

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| nomemic |  |  |

## Selected References

- Gail et al, JNCI 1999; 91: 1829-1846 (tamoxifen risk/benefit)
- Gail, M.H. and Pfeiffer, R.M. Biostatistics 2005; 6: 227239 (risk distribution and expected loss)
- Gail, M.H. JNCI 2008;100:1037-41 (SNP AUC)
- Gail, M.H. JNCI 2009;101:959-963 (SNP value in applications)
- Gail, M.H., Stat. \& Its Interface, 2009;2:117121(resource allocation)
- Park et al, JCO 2012; 30: 2157-62 ("foreseeable SNPs")
- Petracci, E. et al, JNCI 2011;103:1-12
- Rose, G. The strategy of preventive medicine, Oxford University Press, 1992
- Wu et al, AIM 2012; 157: 597


## Additional References on SNPs for Breast Cancer Risk Models

- Pharoah et al Nature Genetics 2002;31:33-36
- Pharoah et al NEJM 2008;358:2796-2803
- Wacholder et al NEJM 2010;362:986-93
- Park et al Nature Genetics 2010;42:570575


## Relative Risk for Breast Cancer

 age 40Menarche age 14
Nulliparous
No biopsies
Mother had breast cancer
baseline risk increased risk baseline risk increased risk

Relative risk $=2.76$ compared to a 40 year old woman with all risk factors at baseline.

| Strong Breast Cancer Risk Factors |  |  |
| :--- | :--- | :---: |
| Factor | Comparison | Relative Risk |
| Age 70-74 | $25-29$ | 56 |
| BRCA1 | No mutation | $2.3-24$ |
| BRCA2 | No Mutation | $4 ; 12-18$ |
| Chest radiation <br> (>40 Gy) | No chest radiation | 6 |
| Contralateral breast cancer <br> Western Country <br> \% Mammographic density $>45 \%$ | None | Rural China |
|  | $<5 \%$ | 5 |

## Moderately Strong Risk Factors

| Factor | Comparison | Relative Risk |
| :---: | :---: | :---: |
| Affected $1^{\text {st }}$ degree relatives |  |  |
| 1 | None | 1.4-3 |
| 2 or more | None | 2.2-5 |
| 1 at age <40 | 1 at age $\geq 60$ | 1.3-2.8 |
| Biopsies |  |  |
| Non-proliferative | None | 1.5 |
| Proliferative | None | 2 |
| Atypical hyperplasia | None | 2-4 |
| HRT for 5 y | None | 1.3-2 |
| Age at first birth $\geq 30 y$ | <20y | 1.8 |

## Weak Risk Factors

| Factor | Comparison | Relative Risk |
| :--- | :--- | :---: |
| Age at menarche $<12 \mathrm{y}$ | $\geq 14 \mathrm{y}$ | 1.2 |
| Age at menopause 55 y | 50 y | 1.15 |
| BMI (kg/m²) |  |  |
| $>30$, post-menopausal <br> $>30$, pre-menopausal | $<21$ | 1.3 |
| Ethanol, 1-2 drinks/d | $<21$ | 0.6 |
| Adverse SNP in FGFR2 | None | 1.13 |

## Some Choices in Risk Modeling

- Genetic model versus empirical model
- Choice of risk factors
- Detailed family history
- Reproductive history (e.g. age at first live birth)
- Medical history (e.g. biopsies, mammographic density)
- Data sources and "piecing together" the model
- Target population: e.g. general population in UK or in US; or high risk clinic


## Genetically-based Models

- Autosomal dominant
- Use extensive family history and BRCA1/2 data
- BRCAPRO (Berry et al, JNCI 1997)
- Claus Model (Claus et al, Cancer,1994)
- Autosomal dominant \& residual familial effects
- BOADICEA, Antoniou et al, BJC 2008
- IBIS, Tyrer, Duffy and Cuzick, Stat Med 2005

This model includes other factors such as LCIS, age at first live birth.

## NCl's Breast Cancer Risk Assessment Tool, BCRAT ("Gail Model")

- Relative risks from Breast Cancer Detection Demonstration Project (BCDDP)
- Incorporates ethnicity-specific SEER data
- Risk factors
- Age
- Age at menarche
- Age at first live birth
- Number of biopsies (and whether atypical hyperplasia is present)
- Number affected mother or sisters

Percentage of 40-49 year old women with breast cancer risk greater than a 50-year old woman without risk factors


Unpublished data related to Wu, Graubard, Gail, AIM 2012

## Summary for Tamoxifen

- Young women at high risk stand to benefit most
- Women without uterus have more favorable risk benefit ratio
- There is no single risk level (e.g. 1.67\%) that applies to all women. Decision depends on age and risks of other outcomes.

Benefit/risk indices for tamoxifen and raloxifene for white non-Hispanic women without a uterus

| 5-year risk | Tamoxifen |  |  | Raloxifene |  |  | Strong evidence of benefits outweighing risks |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 50-59 | 60-69 | 70-79 | 50-59 | 60-69 | 70-79 |  |
| 1.5 | 3 | -53 | -93 | 27 | 2 | -4 |  |
| 2.0 | 31 | -26 | -66 | 49 | 23 | 18 |  |
| 2.5 | 57 | 2 | -39 | 71 | 45 | 40 |  |
| 3.0 | 84 | 29 | -12 | 92 | 67 | 62 | Moderate evidence of benefits outweighing risksBenefits do not outweigh risks |
| 3.5 | 111 | 56 | 15 | 114 | 88 | 82 |  |
| 4.0 | 138 | 83 | 42 | 134 | 109 | 104 |  |
| 4.5 | 164 | 109 | 69 | 156 | 131 | 126 |  |
| 5.0 | 191 | 136 | 96 | 178 | 152 | 147 |  |
| 5.5 | 218 | 163 | 121 | 199 | 173 | 168 |  |
| 6.0 | 244 | 189 | 148 | 220 | 195 | 190 |  |
| 6.5 | 270 | 215 | 175 | 242 | 216 | 210 |  |
| 7.0 | 297 | 242 | 201 | 262 | 237 | 232 |  |
| 5-year projected risk of IBC is $\geq 1.67 \%$. | Using BCPT data and WHI baseline rates |  |  | Combining RR from BCPT and STAR using WHI baseline rates |  |  |  |

Freedman A N et al. JCO 2011;29:2327-2333

## Calibration of BCRAT in the Breast Cancer

 Prevention Trial (Costantino et al, JNCI 1999)| Age <br> Group | $\#$ <br> women | O | E | E/O |
| :--- | :--- | :--- | :--- | :--- |
| $<=49$ | 2332 | 60 | 55.9 | 0.9 |
| $50-59$ | 1807 | 43 | 48.4 | 1.1 |
| $>=60$ | 1830 | 52 | 54.7 | 1.1 |
| All <br> ages | 5969 | 155 | 159.0 | 1.0 |

## Model Validation

- Use independent cohort data to validate
- Calibration
- Does the model correctly predict the number of cancers that develop?
- Discriminatory accuracy
- AUC= the probability that a randomly selected case will have a larger predicted risk than a randomly selected control


## Model Validation

- Use independent cohort data to validate
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- Does the model correctly predict the number of cancers that develop?
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## Designing Prevention Trials

- Statistical power
- Depends on the number of events
- Number of events is proportional to average absolute risk of trial participants
- Eligibility criteria
- Select subjects who stand to benefit from intervention
- Increase efficiency of trial by including high risk subjects
- Examples: BCPT (P-1) Trial, STAR Trial



## Usefulness of SNPs for Breast Cancer Risk Models

- Increase discriminatory accuracy (AUC)?
- In public health applications?
- Selected references
- Gail and Pfeiffer, Biostatistics, 2005
- Gail, JNCI 2008, 2009
- Wacholder et al, NEJM 2010
- Park et al, JCO, 2012


## The Strategy of Preventive Medicine ${ }^{1}$

- The population strategy of prevention
- The "high-risk" strategy
${ }^{1}$ Geoffrey Rose, Oxford University Press, 1992


## Absolute ("Crude") and "Pure" Risk in 1000 60-Year Old Women

| Age at <br> Start of <br> Interval | \# At Risk | \# Incident <br> Breast <br> Cancer | \# Deaths <br> from Other <br> Causes |
| :---: | :---: | :---: | :---: |
| 60 | 1000 | 17 | 44 |
| 65 | 939 | 20 | 63 |
| 70 | 856 | 22 | 89 |
| 75 | 745 | $\ldots$. | $\ldots$. |

Absolute risk of breast cancer to age $75=$ (17+20+22)/1000 = 5.9\%
"Pure" risk = 1- (1-17/1000)(1-20/939)(1-22/856)

$$
=6.3 \%
$$

## Absolute Risk Calculation for Woman with Risk Factors X

## $R(a, \tau, x)=$

$\int_{a}^{a+\tau} h_{1}(t) r r(t, x) \exp \left[-\int_{a}^{t}\left\{h_{1}(u) r r(u, x)+h_{2}(u)\right\} d u\right] d t$
$h_{1}(t)$ is baseline hazard of breast cancer incidence
$h_{2}(t)$ is mortality hazard from competing risks
$\operatorname{rr}(\mathrm{t} ; \mathrm{x})=\exp \left\{\cos ^{\top} \mathrm{x}(\mathrm{t})\right\}$ is relative risk of breast cancer for covariates $\mathrm{x}(\mathrm{t})$

## Factors Affecting Absolute Breast Cancer Risk

- Factors that increase absolute risk
- Increasing the risk projection interval
- Increased age at the beginning of the projection interval (usually)
- Having multiple or strong risk factors for breast cancer
- Factors that decreases absolute risk
- Mortality from non-breast cancer causes


## BCRAT for Ethnic/Racial Groups

- Special models have been developed for African-American (JNCI, 2007) and AsianAmerican (JNCI, 2011) women
- Work needed for Hispanic women and other subgroups
- BCRAT calibrates to SEER data for subgroups


## Individual Breast Cancer Risk Projections

Current age (20-80): 40
Upper age limit (20-80): 50
Age at menarche: 12
Age at first live birth (0 if no live birth): 0
Number of previous breast biopsies: 1
At least one biopsy with hyperplasia (y:yes, n:no, u:unknown): u
Number of first degree relatives (mother or sister(s)) with breast cancer: 0
Absolute risk $=3.6 \%$ with $95 \%$ CI $=(3.0 \%, 4.3 \%)$

## Model with Perfect Discriminatory Accuracy

- Treat only the 246.6 women destined to get breast cancer
- Breast cancers $\quad 246.6 \times .51=125.8$
- Net adverse effects $(55.9+326.4+174.9+150.5) \times 246.6 / 10^{5}=1.7$
- Events among those not destined to get breast cancer and therefore not treated (589.6-246.6)x\{(100,000-246.6)/105\}= 342.2
- Grand total 469.7


## Threshold Risk r* for Optimal Decision

Expected net benefit from tamoxifen for woman with BC risk r
$r(1-0.51)+101.6(1-0.55)+81.4(1-4.01)+110.0(1-1.59)+50.0(1-3.01)$
$=0.49 r-364.7$.

Expected net benefit positive if $r>364.7 / 0.49=774.3 \equiv r^{*}$

Only give tamoxifen if $r>774.3 / 10^{5}$. This is a "high-risk" strategy, because only $1 \%$ of women aged 50-59 have risks this high.

## Summary (Continued)

## - Public health applications

- Designing Prevention Trials
- Assessing absolute risk reduction from prevention
- To implement "high risk" prevention strategy
- Find safer interventions that can be used broadly
- Increase discriminatory accuracy
- Model risks of the several health outcomes
- Allocating scarce resources
- Cost of risk assessment should be small
- Improvements from SNPs small in these applications. Allocating scarce resources



## Women in Forties with Absolute Risk of a 50 -Year Old Woman

- Consider screening mammography because these women have nearly the same prevalence of detectable cancer and intervention effect as the 50 -year old woman (Gail and Rimer, JCO,1998)
- $74 \%$ of white women in 40 's have at least the risk of 50 -year old woman with no risk factors (Wu, Graubard, Gail, AIM, 2012)
- "Tipping the Balance" (van Ravesteyn et al, AIM 2012)


## Mammographic Screening of a Population under Cost Constraints

- Screening reduces the number of deaths from $N \mu$ to $N \mu(1-\rho)$, a reduction of $N \mu \rho$ deaths
- We take as the unit of cost, the total cost required to screen the entire population, $\mathrm{NC}_{\mathrm{S}}=1$. The fraction of this total cost that is available for the screening program is $\mathrm{h} \leq 1$.
- We perform a risk assessment on members of the population to decide who should get screening. Risk assessment costs
$C_{R}=k C_{S}$, where $k$ is the cost ratio of risk assessment to screening.


## Using Risk Models to Allocate Mammograms under Cost Constraints

- Perform a risk assessment
- Allocate mammograms to those with high risks
- Optimal strategy
- h is the fraction of needed money available
$-k$ is the cost ratio for risk assessment:
- $g$ is proportion given risk assessment
- p is proportion assessed who are given mammograms
$-m$ is proportion given mammogram at random among those without risk assessment

Fraction of Maximal Attainable Lives Saved, B, versus Resources, h

B

h
Lives Saved
$N \mu-N g \int_{0}^{\xi_{1-p}} r d F(r)-N g(1-\rho) \int_{\xi_{1-p}}^{1} r d F(r)$
$-N(1-g) \mu m(1-\rho)-N(1-g)(1-m) \mu$
$=N \mu \rho[g\{1-L(1-p)\}+(1-g) m]$
where $\xi_{1-p}=F^{-1}(1-p)$.
Fraction of the maximum possible lives saved
$B=g\{1-L(1-p)\}+(1-g) m$

## Goal

Maximize the proportion of lives saved, compared to giving all women mammograms, $g\{1-L(1-p)\}+(1-g) m$, subject to cost constraints
$g k+g p+(1-g) m \leq h$

## Four Basic Strategies

- Assess risk in all and screen a top proportion p of those assessed until the remaining money is used. ( $g=1, p>0, m=0$ )
- Assess risk in a fraction $\mathrm{g}<1$ and use all the remaining money to screen a top proportion $p$ of those assessed. ( $0<\mathrm{g}<1, \mathrm{p}>0, \mathrm{~m}=0$ )
- Assess risk in a fraction $g<1$, screen a top proportion $p$ of those assessed and a random sample of a proportion $m>0$ of the un-assessed. ( $0<\mathrm{g}<1, \mathrm{p}>0, \mathrm{~m}>0$ )
- Screen as many as possible at random with no risk assessment. ( $\mathrm{g}=0, \mathrm{~m}>0$ )


Optimal Strategy is: (1) $g=1$ (Black); (2) $0<g<1, m=0$ (Dark Grey); (3) $0<g<1, m>0$ (Light Grey); or (4) $g=0$ (White).

| $\begin{array}{ll}\text { Allocating Mammograms When Only } \\ \text { Enough Money for Half the Population }\end{array}$ |  |  |
| :--- | :--- | :--- |
| Risk | $\begin{array}{l}\text { Proportion of lives } \\ \text { assessment }\end{array}$ | $\begin{array}{c}\text { \% Improvement } \\ \text { saved compared to } \\ \text { giving mammograms } \\ \text { to all women }\end{array}$ |
| Norsus no risk |  |  |
| assessment |  |  |$\}$


| Allocating Mammograms When Only Enough Money for Half the Population |  |  |
| :---: | :---: | :---: |
| Risk assessment | Proportion of lives saved compared to giving mammograms to all women | \% Improvement versus no risk assessment |
| None | 0.500 |  |
| BCRAT ${ }^{\text {a }}$ | 0.632 | 26.4\% |
| BCRATplus7SNPs | NPs ${ }^{\text {b }} 0.667$ | 33.4\% |
| ${ }^{\mathrm{a}}$ AUC=0.607; ${ }^{\text {b }}$ AUC $=0.632 ; \mathrm{k}=0.02$ |  |  |
| Gail, Statistics and Its Interface, 2009 |  |  |

## Key Role of Distribution of Risk, $F(r)$, in the Population

$R(x)$ is risk for person with covariates, $x$

$$
F(r)=P(R \leq r)=\int_{x: R(x) \leq r} d F_{X}(x)
$$

From $F(r)$, compute
Distribution of risk in cases and in non-cases Functionals of $F$ like AUC
Expected losses for decision-making
References
Gail \& Pfeiffer, Biostatistics 2005;6:227-239
Gail, JNCI 2008;100:1037-1041
Gail, JNCI 2009;101:959-963

## Distributions of risk in cases and controls and the Lorenz curve

Distribution $G$ of risk in cases
$\mu=\int_{0}^{1} r d F(r)=P(Y=1)$
$G(r)=P(R \leq r \mid Y=1)=\frac{1}{\mu} \int_{0}^{r} u d F(u)$
Lorenz curve of $F$ is $L(p)=\mu^{-1} \int_{0}^{F^{-1}(p)} r d F(r)=G\left(F^{-1}(p)\right)$
$F_{\text {control }}(r)=P(R \leq r \mid Y=0)=\frac{1}{1-\mu} \int_{0}^{r}(1-u) d F(u)$

Key Assumptions to Compute F

- Hardy-Weinberg equilibrium
- Linkage equilibrium across SNPs

$$
P(\mathbf{X})=\prod_{i=1}^{\prime} p_{i}\left(X_{i}\right)
$$

- Additive effects of disease alleles
- Odds ratios multiply across SNPs

$$
r r(\mathbf{X})=\prod_{i=1}\left(O R_{i}\right)^{x_{i}}
$$

- SNP ORs multiply BCRAT ORs
- SNPs independent of factors in BCRAT


ROC-Type Curves to Assess Discriminatory Accuracy of Risk Models


## Uses of Absolute Risk for the Individual Patient

- General perspective in counseling
- Making clinical decisions for preventive interventions with risks and benefits
- Clinical management after diagnosis (prognostic risk models)


## Individual Breast Cancer Risk Projections

Current age (20-80): 40
Upper age limit (20-80): 50
Age at menarche: 12
Age at first live birth (0 if no live birth): 0
Number of previous breast biopsies: 1
At least one biopsy with hyperplasia (y:yes, n:no, u:unknown): u

Number of first degree relatives (mother or sister(s)) with breast cancer: 0

Absolute risk $=3.6 \%$ with $95 \% \mathrm{CI}=(3.0 \%, 4.3 \%)$

## Preventive Action Applied Throughout the Population

- Must be very safe
- Usually has the greatest potential for disease prevention
- Examples
- Reduce environmental or occupational exposure
- Behavioral change: e.g. more exercise or decreased alcohol
- Take an hypothetical safe cancer preventive agent


## Preventive Action Applied To High Risk Subgroup

- Useful if intervention poses adverse side effects or risks
- Useful if intervention is too costly for widespread use
- Limited potential for disease prevention
- Examples
- Tamoxifen to prevent breast cancer
- Oophorectomy and/or prophylactic mastectomy
-MRI screening


## Enhancing Effectiveness of High Risk Strategy

- Increase discriminatory accuracy of risk model to concentrate most of the cases in a small high risk group
- Find interventions with less toxicity that can be applied to a larger high risk subgroup (e.g. raloxifene, aromatase inhibitors?) (Cuzick, Breast Cancer 2008)
\% of general population aged 50-59



## Other Breast Cancer Risk Models

- Based on detailed family history
- Rare autosomal dominant transmission only
- Claus (Cancer,1994)
- BRACAPRO (can incorporate BRCA genotype)

Berry, JNCI 1997

- Rare autosomal dominant plus residual familial aggregation
- BOADICEA (polygenic, can incorporate BRCA genotype) Antoniou BMJ 2004,2008
- Tyrer, Duff, Cuzick (common dominant and nongenetic risk factors) Stat Med 2004


## Other models (continued)

- Family history plus other factors
- Rosner (detailed reproductive history) JNCI 1996
- Mammographic density
- Chen (BCRAT risk factors) JNCI 2006
- Barlow (BI-RADS, fam. Hx, biops) JNCI 2006
- Tice (BI-RADS, fam. Hx, race, biops) Ann Int Med 2008
- SNPs plus BCRAT

Gail JNCI 2008,2009; Pharoah NEJM 2008

## - Biopsy Histopathology

Hartmann, JCO 2007

## Distribution of Risk in Women aged 50-59 years



Note that only $1.0 \%$ of women in this age group satisfy BCRAT > r*.

## Some standard criteria for evaluating the performance of risk models

- Calibration: Are risk estimates unbiased?
- Discrimination: How different are the distributions of risk among individuals who do and do not develop the disease (concordance or AUC)?
- Accuracy: How well does model categorize individuals (PPV, NPV, Proportion Correctly Classified)?


## Modest Discriminatory Power

Rockhill et al., JNCI 2000

## Distribution of breast cancer risk among cases and controls derived from National Health Interview Survey Data



## Comments on Area Under ROC (AUC)

- Can be estimated from case-control data
- Hard to increase
- Incorporation of mammographic density, a strong risk factor, only increases from e.g. 0.60 to 0.66 for 60-64 yrs women (Chen, ... Gail, submitted)
- Comparable to AUC for age-specific AUC for cardiovascular risk models


## Can a model with modest discriminatory value be useful for screening? For deciding whether or not to intervene?

$$
\begin{aligned}
& \begin{array}{l}
\text { Sensitivity and specificity of decision } \\
\text { rule } \delta=1 \text { if } r \geq \mathrm{r}^{*} \text { and } \delta=0 \text { otherwise }
\end{array} \\
& \begin{aligned}
\operatorname{sens}\left(\mathrm{r}^{*}\right) & =P(\delta=1 \mid Y=1)=P\left(r \geq \mathrm{r}^{*} \mid Y=1\right) \\
& =1-\mathrm{F}_{\text {case }}\left(\mathrm{r}^{*}\right)
\end{aligned} \\
& \begin{aligned}
\operatorname{spec}\left(\mathrm{r}^{*}\right) & =P(\delta=0 \mid Y=0)=P\left(r<\mathrm{r}^{*} \mid Y=0\right) \\
& =\mathrm{F}_{\text {control }}\left(\mathrm{r}^{*}-\right)
\end{aligned}
\end{aligned}
$$




ROCs for various risk factor odds ratios. From Pepe et al. AJE 2004

## Model Assessment Based on Population of N Subjects

- $Y_{i}=1$ if cancer develops in time specified interval, 0 otherwise, $i=1,2, \ldots \mathrm{~N}$
- $X_{i}$ are covariates for subject $i$
- $r\left(X_{i}\right)$ is previously developed absolute risk model designed to estimate $P\left(Y_{i}=1\right)$
- $\pi_{i}$ is the true $P\left(Y_{i}=1\right)$

Gail and Pfeiffer, Biostatistics, 2005

## Assessing Model Calibration

Goodness-of-fit criteria based on comparing observed (O) with expected (E) number of events overall and in subgroups $A_{1}, A_{2}, \ldots$ of the population

$$
\begin{aligned}
O_{k} & =\sum_{i=1}^{N} Y_{i} I\left(X_{i} \in A_{k}\right) \\
E_{k} & =\sum_{i=1}^{N} r\left(X_{i}\right) I\left(X_{i} \in A_{k}\right)
\end{aligned}
$$

If $r$ is well calibrated, $O_{k}$ has mean $E_{k}$

## Specific Loss Function-Based Approach to Model Assessment

Two applications:
-Screening
-Weighing risks and benefits of an intervention

Gail and Pfeiffer, Biostatistics 2005

## Expected Loss

$$
\begin{aligned}
& E L=C_{11} P(Y=1, \delta=1)+C_{01} P(Y=1, \delta=0) \\
& +C_{10} P(Y=0, \delta=1)+C_{00} P(Y=0, \delta=0) \\
& =C_{11} \int_{r^{*}}^{1} r d F(r)+C_{01} \int_{0}^{r^{*}} r d F(r)+C_{10} \int_{r^{*}}^{1}(1-r) d F(r)
\end{aligned}
$$

## Decision to Intervene

$\delta=1$ if decide to intervene, $\delta=0$ otherwise.
"Intervention" changes distribution of health outcomes.

Consider two outcomes for tamoxifen intervention:
$Y_{1}=$ breast cancer
$\mathrm{Y}_{2}=$ stroke
$P\left(Y_{1}=i, Y_{2}=j \mid \delta=0\right) \neq P\left(Y_{1}=i, Y_{2}=j \mid \delta=1\right)$

## Example: Breast Cancer, Stroke and Intervention by Tamoxifen

STROKE: No covariate model for stroke risk; use average age-specific risk s
$r_{001}(x)=\mathrm{s}, r_{101}(x)=1.6 s$

## BREAST CANCER:

$r_{010}(x)=$ Gail model estimate for breast cancer
$r_{110}(x)=0.5 r_{010}(x)$
$r_{011}(x)=r_{111}(x)=0$

## Assessing Model Calibration

The model $r(x)$ is perfectly calibrated (unbiased) if for each x

$$
r(x)=E(\pi \mid x)=\int \pi d G(\pi \mid x)
$$

Then
$\int_{0}^{1} r d F(r)=\int_{x} E(\pi \mid x) d G_{x}(x)=E(\pi)=P(Y=1)$
Unbiased (well calibrated) in the whole population

$$
\frac{1}{N} \sum_{i=1}^{N} Y_{i} \approx \int_{0}^{1} r d F(r)=\mu
$$

## Extend Notation to Intervention Setting

True event probabilities for bivariate outcomes for $\delta=0,1$

$$
\begin{aligned}
\pi_{\delta i}=\{ & P_{\delta}\left(Y_{\delta 1 i}=1, Y_{\delta 2 i}=1\right), P_{\delta}\left(Y_{\delta 1 i}=1, Y_{\delta 2 i}=0\right) \\
& \left.P_{\delta}\left(Y_{\delta 1 i}=0, Y_{\delta 2 i}=1\right), P_{\delta}\left(Y_{\delta 1 i}=0, Y_{\delta 2 i}=0\right)\right\}^{T}
\end{aligned}
$$

Risk models to predict quadrinomial outcomes in presence and absence of intervention ( $\delta=0,1$ )

$$
\left.r_{\delta}(x)=\left\{r_{\delta 11}(x), r_{\delta 10}(x), r_{\delta 01}(x), r_{\delta 00}(x)\right)\right\}^{T}
$$

## Measures of Discrimination

- ROC curve (plot of sensitivity against 1specificity)
- Area under the ROC curve (AUC)
- Concordance statistic (Rockhill et al, 2001; Bach et al, 2003)
- ~ (Gini index+1)/2 for rare events
- Partial area under the curve (Pepe, 2003; Dodd\&Pepe, 2003)


## Assessing Model Accuracy

For clinical decision making a decision rule is needed to classify subjects

$$
\delta_{i}=\left\{\begin{array}{lc}
1, & \text { if } r \geq r^{*} \\
0, & \text { otherwise }
\end{array}\right.
$$

for some threshold $\mathrm{r}^{*}$

## Accuracy Criteria

- Positive predictive value
- Negative predictive value
- Weighted combinations of both, eg
$P($ correct decision $)=P\left(r \geq \geq^{*}\right) P\left(Y=1 \mid r \geq r^{*}\right)+$ $P\left(r<r^{*}\right) P\left(Y=0 \mid r<r^{*}\right)$
Depend on sensitivity, specificity, and $P(Y=1)$
Cannot be estimated from samples of cases and controls alone


## An Alternative Approach to Incorporate Covariates*

- Model $\mathrm{F}_{1}(\mathrm{t} ; \mathrm{X})=(\mathrm{T} \leq \mathrm{t}$ from cause $1 \mid \mathrm{X})$ directly via $g\left\{F_{1}(t ; X)\right\}=v_{0}(t)+X \beta$
- Use counting process methods, but "risk set" at $t$ consists of those who have not failed plus those who failed earlier but not from cause 1
* Fine and Gray, JASA 1999


## Fine, JP and Gray RJ, JASA 1999

- $F(t \mid X)=$ absolute risk to age $t$ given $X$
- $g\{F(t \mid X)\}=h_{0}(t)+X \beta$
- E.g. $g(u)=\log \{-\log (1-u)\}$
- $\lambda=$ hazard $=\{\mathrm{dF}(\mathrm{t} \mid \mathrm{X}) / \mathrm{dtt}\} /(1-\mathrm{F}(\mathrm{t} \mid \mathrm{X}))$
- Issues
- No cause-specific interpretation
- Requires cohort data
- Complex estimation with censoring

Advantages of Cause-Specific Relative Risk Model for Covariates

- Familiar interpretation of cause-specific relative risks
- Standard survival methods for estimation with cohort data
- Possible to use different data sources:
- Relative risks from case-control or case-cohort data
- Baseline hazard $h_{1}(t)$ from SEER data via $h_{1}(t)=h_{1}{ }_{1}(t)\{1-A R(t)\}$,
where $\mathrm{h}^{\star}{ }_{1}(\mathrm{t})$ is the incidence rate in SEER
- For alternative modeling, see Fine and Gray (JASA, 1999)

